



# Probabilistic Graphical Models for Recommendation in Social Media

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- Social networks have been used widely in the social and behavioral sciences, in economics, marketing, . . .



- Directed or undirected graph  
nodes: actors  
edges: social relationships or interactions

# Introduction

- Explicit social network relationships provided by users

The Facebook logo, consisting of the word "facebook" in white lowercase letters on a blue rectangular background.The LinkedIn logo, featuring the word "Linked" in black and "in" in white lowercase letters inside a blue square.

- Implicit social network relationships inferred from user interactions
  - Email network
  - Co-worker network

# Introduction

- Emergence of online social networks
- Among the top websites <http://www.alexa.com/topsites>

...

2. FaceBook

The Facebook logo, consisting of the word "facebook" in white lowercase letters on a blue rectangular background.

...

8. LinkedIn

The LinkedIn logo, featuring the word "Linked" in black and "in" in white lowercase letters inside a blue square.

...

10. Twitter

The Twitter logo, featuring the word "twitter" in a light blue, rounded, lowercase font with a white outline.

...

→ Availability of very large datasets

# Introduction

- Users want to have personalized results.
  - But are not willing to spend a lot of time to specify their personal information needs.
  - Recommender systems automatically identify information relevant for a given user, learning from available data.
  - Recommender systems play a crucial role in the evolution of online social networks, e.g. 50% of the links in LinkedIn were recommended by an algorithm.
- [Ester, Tutorial at RecSys 2013]

# Introduction

## Outline

- Introduction
- Item recommendation
  - matrix factorization [RecSys 2010]
  - stochastic block model [RecSys 2011]
- Location recommendation
  - spatial topic model [RecSys 2013]
  - spatio-temporal topic model [ICDM 2013]
- Future work

# Introduction

- Social rating network (SRN)  
(online) social network, where users are associated with item ratings.
- Item ratings can be numeric [1..5] or Boolean (bookmark photo, like article, . . .).
- Examples: Epinions, Flixster, last.fm, flickr, Digg.
- Two types of user actions:  
(1) social actions,  
(2) rating actions.

## Social rating networks

- **Social influence**  
ratings are influenced by ratings of friends,  
i.e. friends are more likely to have similar ratings than strangers.
- **Correlational influence**  
ratings are influenced by ratings of users with similar ratings,  
i.e. if some ratings are similar, further ratings are more likely also similar.

## Social rating networks



- **Selection**  
users relate to users with similar ratings,  
i.e. users with similar ratings are more likely to become friends.
- **Transitivity**  
users relate to friends of their friends,  
i.e. users are more likely to relate to indirect friends  
than to strangers.

## Social rating networks

- Rating prediction
  - Given user  $u$  and target item  $i$ .
  - Predict the rating  $r_{u,i}$ .
- Link prediction
  - Given users  $u$  and  $v$ .
  - Predict the probability  $p_{u,v}$  of a link from  $u$  to  $v$ .
- Top-N recommendation
  - Given user  $u$ .
  - Rank the items  $i$  w.r.t.  $r_{u,i}$  / the users  $v$  w.r.t.  $p_{u,v}$ .

# Recommendation

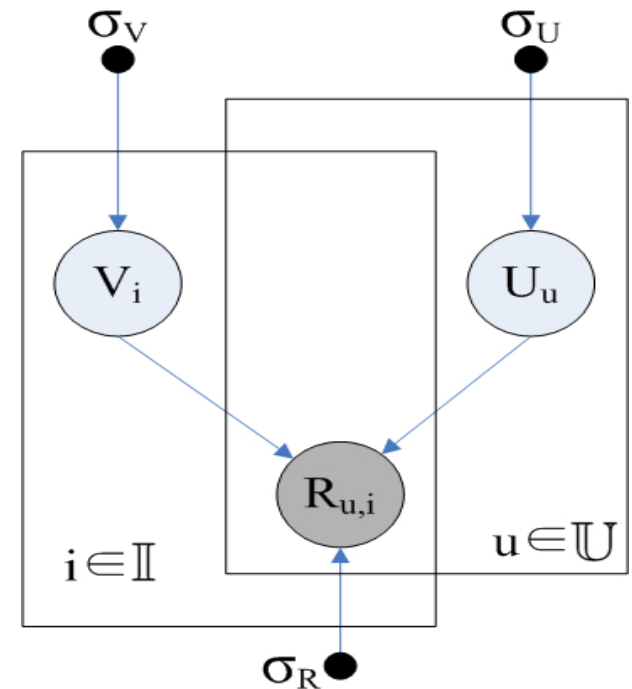
- Collaborative filtering (CF)
- Memory-based approach
  - Determine  $k$  users most similar to  $u$   
and aggregate their ratings of item  $i$ .
- Model-based approach
  - Training: learn model parameters.
  - Test: apply model for rating prediction or top-N recommendation.
- Cold-start problem
  - Cannot deal with new users / users with few ratings.

## Recommendation

- Observed ratings  $R_{ui}$  are governed by latent variables (factors) of users and items.
- Latent factors for users  
 $U \in \mathbb{R}^{K \times N}$
- Latent factors for items  
 $V \in \mathbb{R}^{K \times M}$
- User item ratings

$$p(R|U, V, \sigma_R^2) = \prod_{u=1}^N \prod_{i=1}^M \left[ \mathcal{N}\left(R_{u,i} | g(U_u^T V_i), \sigma_r^2\right) \right]^{I_{u,i}^R}$$

$g$ : logistic function,  $\sigma_u, \sigma_v, \sigma_R$ : normal priors



## Matrix factorization

- Motivation for social network-based recommendation:
  - social influence, selection, and other effects
  - can deal with cold-start users,  
as long as they are connected to the social network.
- Memory-based approach
  - MoleTrust,
  - TrustWalker, . . .
- Model-based approach
  - Matrix factorization (MF)

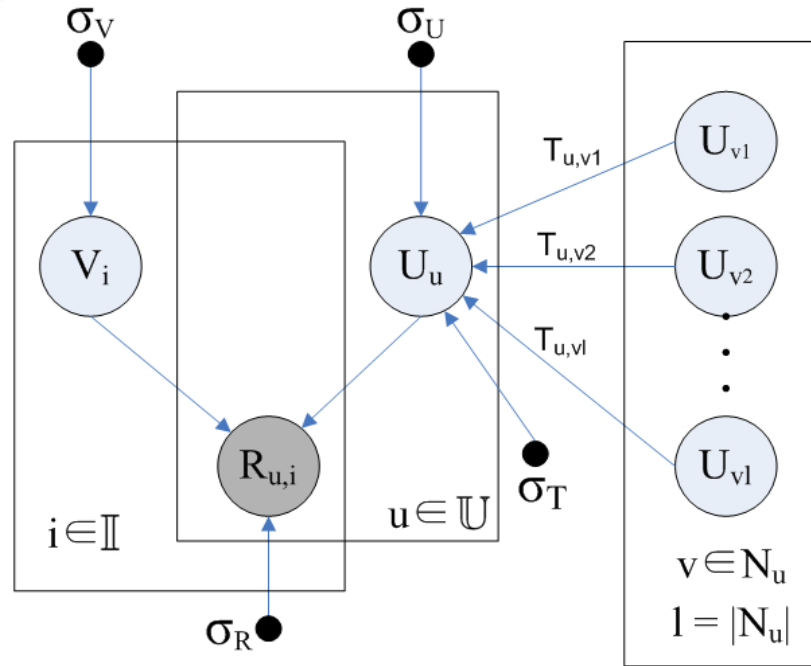
## Recommendation in social networks: a matrix factorization approach

- Social correlation  
behavior of a user  $u$  is correlated with that of his direct neighbors  $N_u$ .
- Latent factors of a user depend on those of his neighbors.

$$\hat{U}_u = \sum_{v \in N_u} T_{u,v} U_v$$

- $T_{u,v}$  is the normalized trust value.
- Trust propagation to indirect neighbors.

## Recommendation in social networks: a matrix factorization approach



$$\sum_{\text{all observed } (u,i)} (R_{ui} - \hat{R}_{ui})^2 + \lambda(\|U\|^2 + \|V\|^2)$$

$$+ \beta \left( \sum_u \left( (U_u - \sum_v T_{u,v} U_v) (U_u - \sum_v T_{u,v} U_v)^T \right) \right)$$

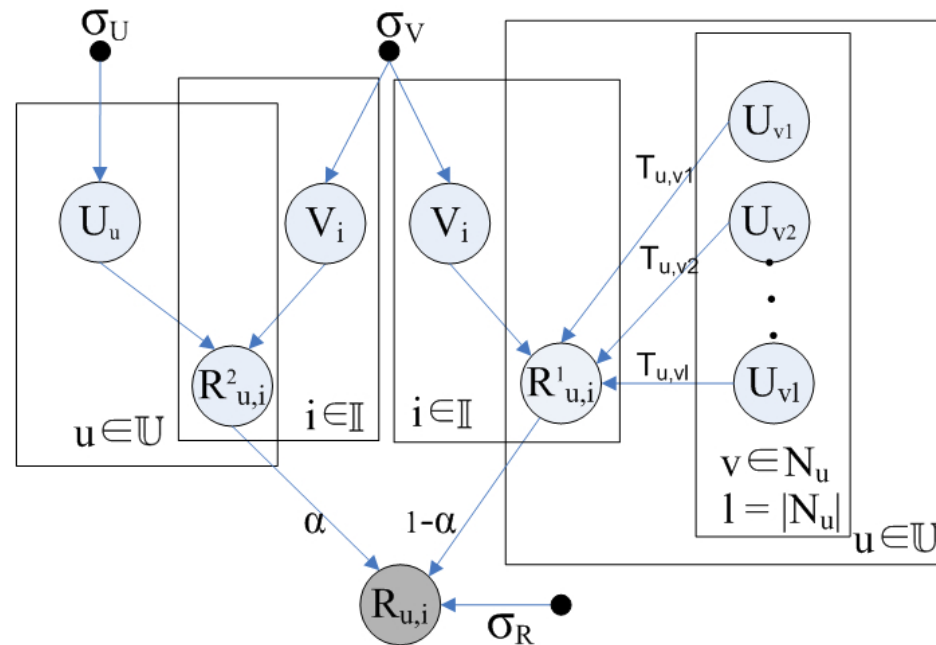
## Recommendation in social networks: a matrix factorization approach

- Comparison partners:
  - CF
  - Baseline MF
  - STE (Social Trust Ensemble) [Ma et al. 2009]
  - SocialMF (our method)
- Datasets:
  - Epinions
  - Flixster
- Number  $k$  of factors:
  - 5 or 10

## Recommendation in social networks: a matrix factorization approach

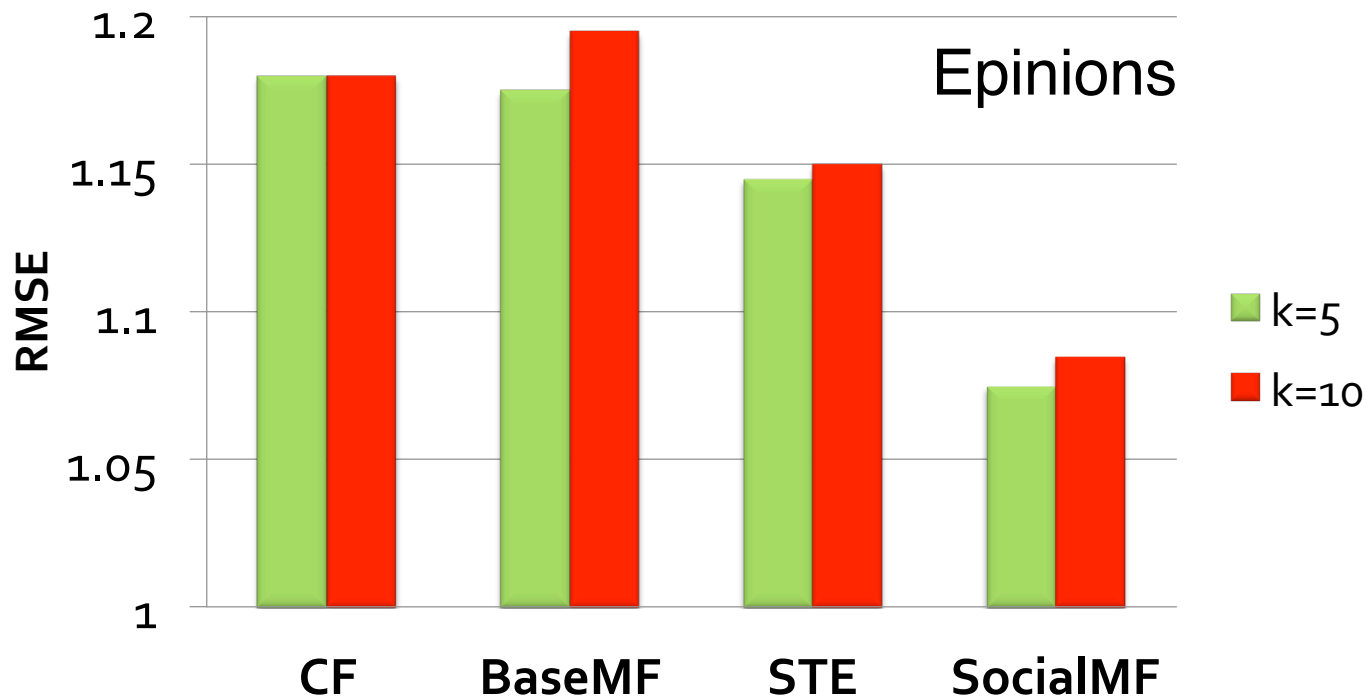


STE



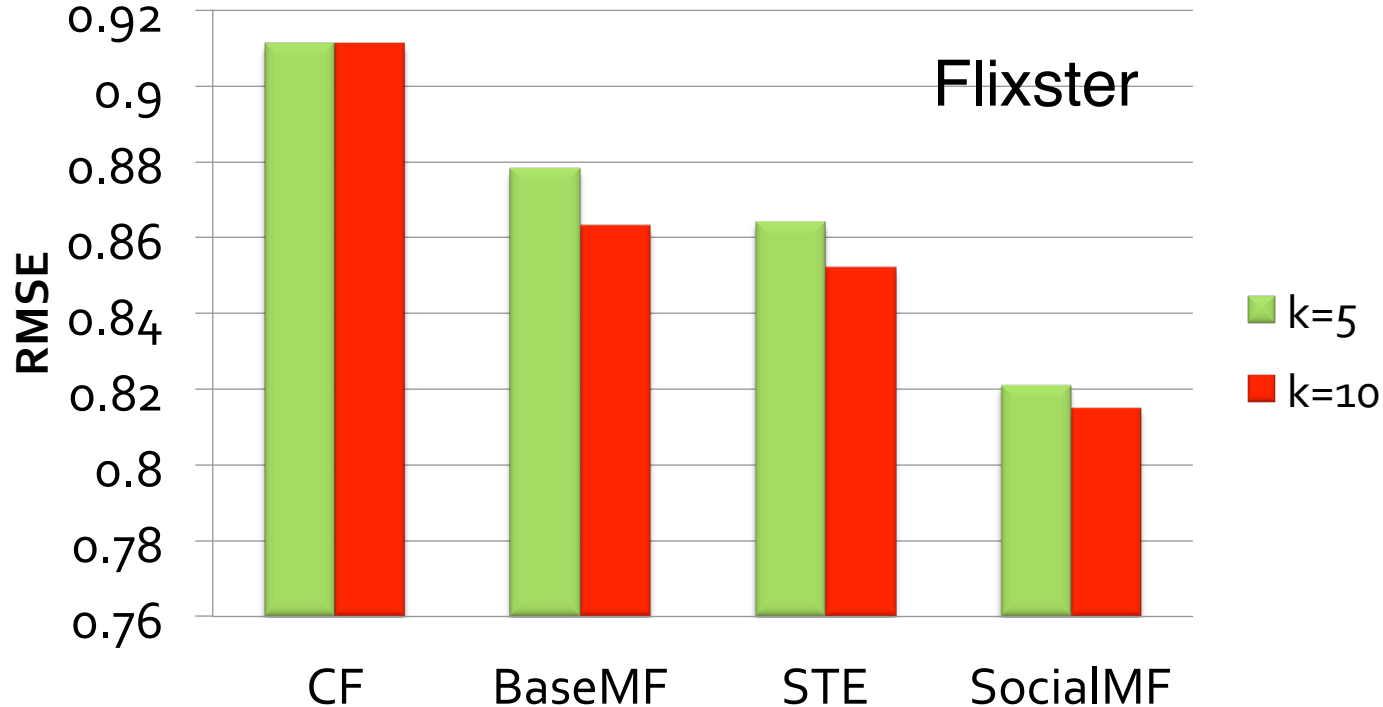
$$\hat{R}_{u,i} = \alpha U_u^T V_i + (1 - \alpha) \sum_{v \in N_u} T_{u,v} U_v^T V_i$$

# Recommendation in social networks: a matrix factorization approach



- Gain over STE: 6.2%. for K=5 and 5.7% for K=10

# Recommendation in social networks: a matrix factorization approach



- SocialMF gain over STE (5%) is 3 times the STE gain over BasicMF (1.5%)

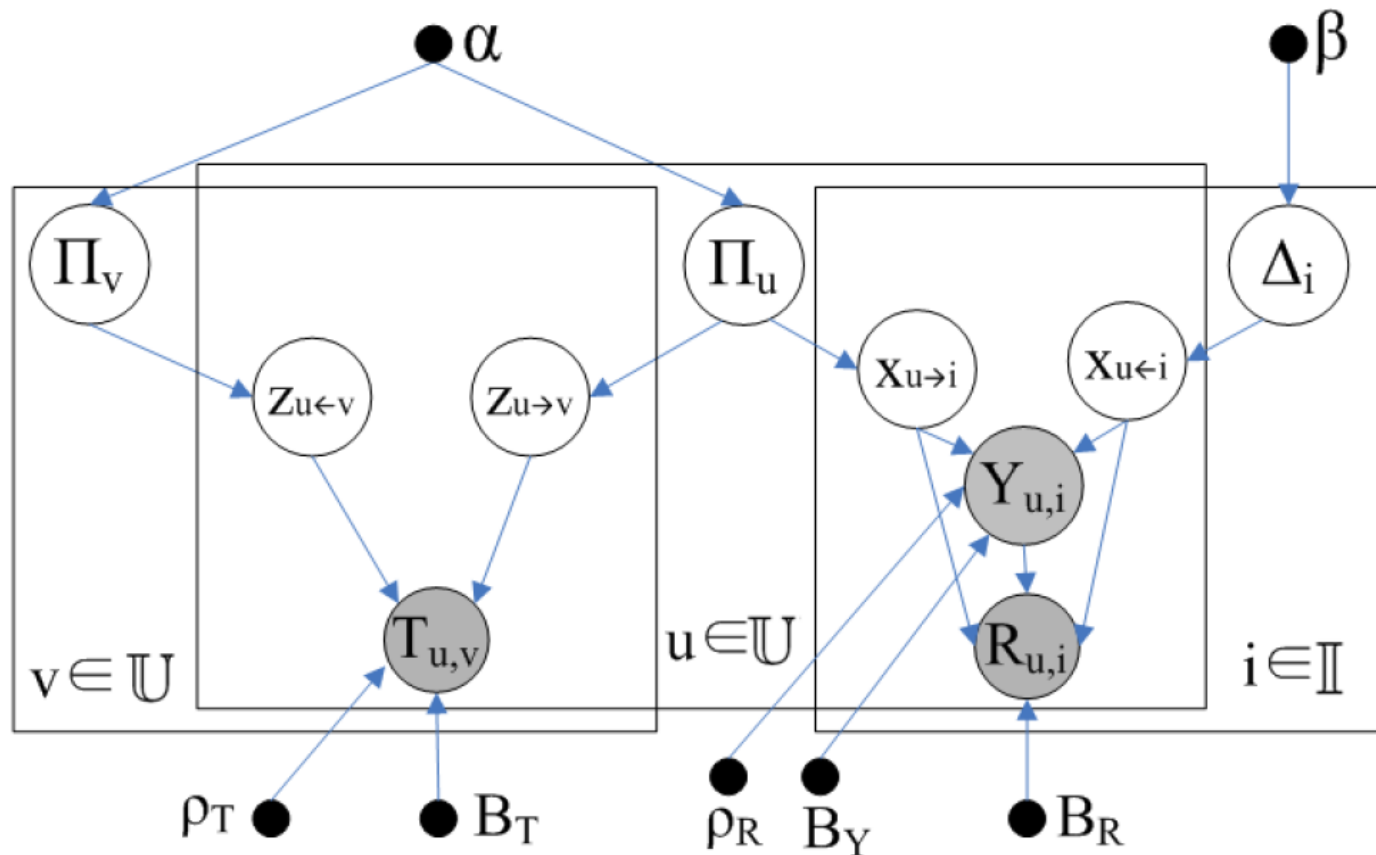
## Recommendation in social networks: a matrix factorization approach

- Social influence and selection happen simultaneously.
  - Leads to formation of communities/clusters.
  - Users within a cluster have similar patterns of actions.
  - Users may belong to different clusters for different types of actions.
- Clustering-based method for recommendation

## Recommendation in social networks: a generalized stochastic block model

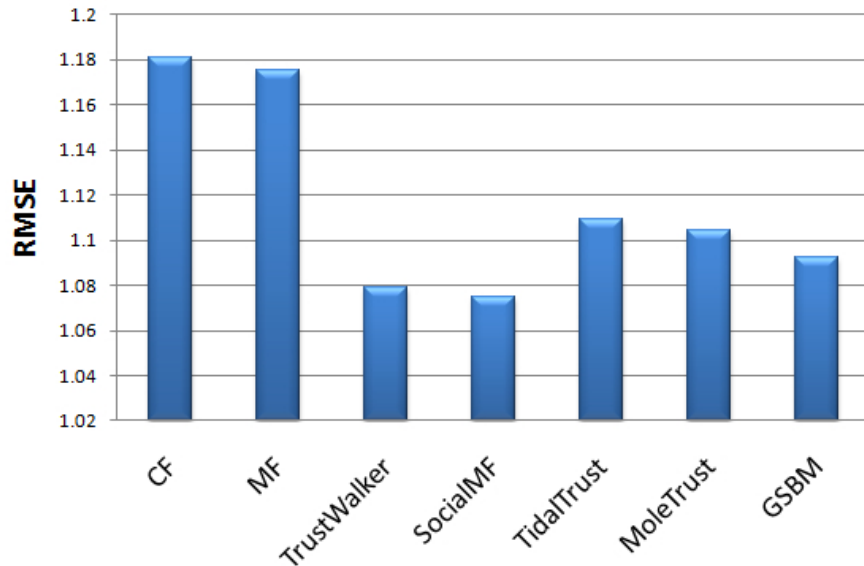
- We extend the mixed membership stochastic block model [Airoldi et al. 2008].
- In each action, users probabilistically act as a member of one of the latent clusters.
- Every item is considered to belong to a latent cluster when it is being rated.
- The relationships between users and items are governed by the relationships between clusters.

## Recommendation in social networks: a generalized stochastic block model

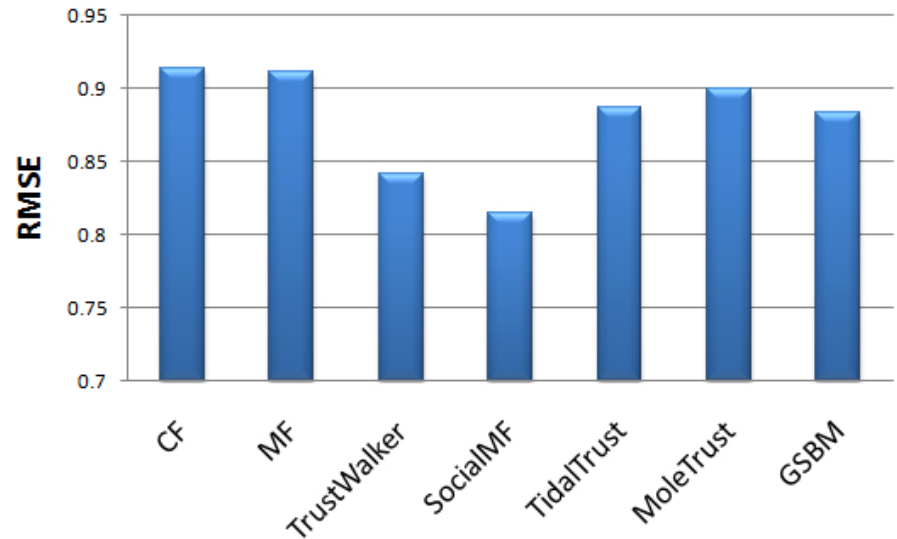


# Recommendation in social networks: a generalized stochastic block model

## Rating prediction



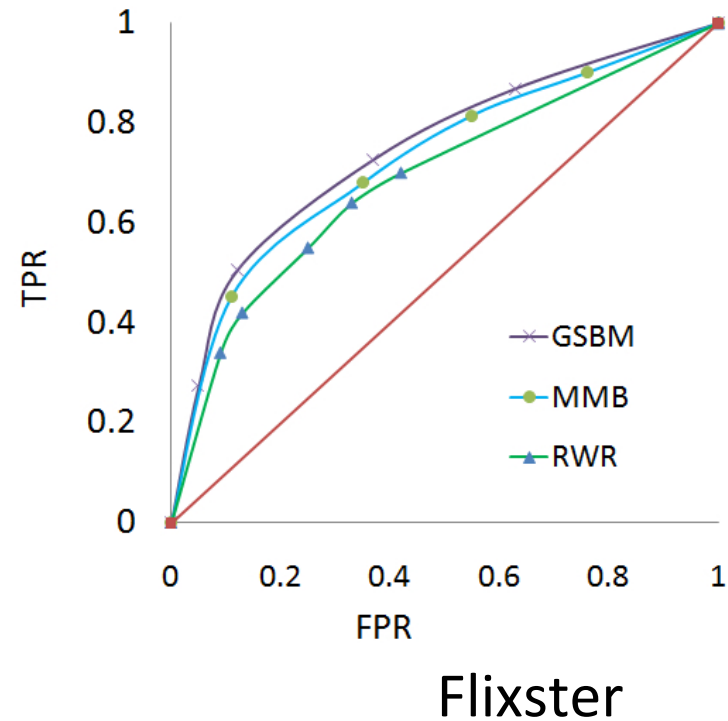
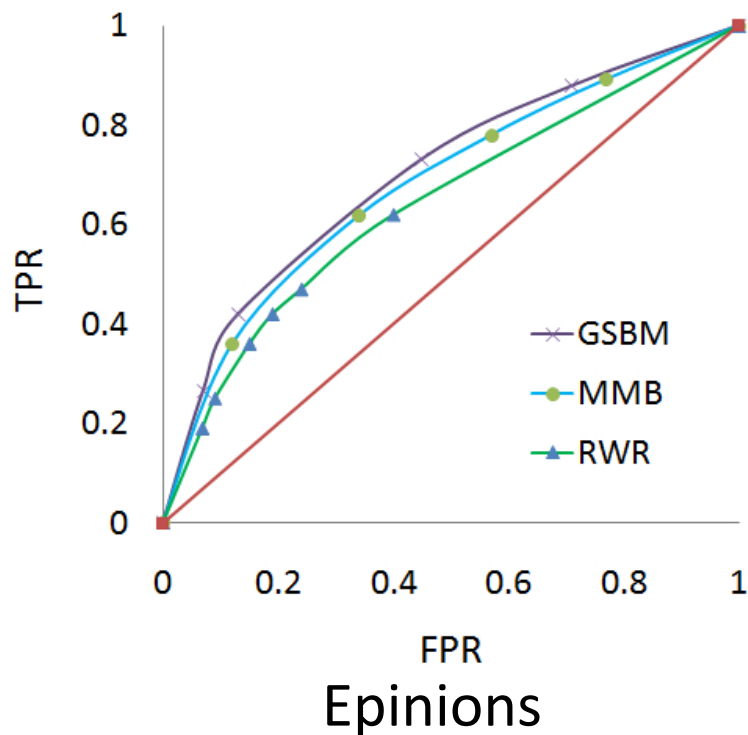
Epinions



Flixster

Recommendation in social networks:  
a generalized stochastic block model

## Link prediction



Recommendation in social networks:  
a generalized stochastic block model



- Location-based social network (LBSN) online social network, where users check in at locations (points of interest).
- Check-in:  
User: @XXX  
Time: 2012-04-23 12:04:09  
Coordinates: 40.7244 -74.0020  
Location: a825251e7c560c1e  
→unique id = store, restaurant, mall, school, . . .  
(Post:  
Close to the equator, perfect soil and high elevation make @CafeD produce the perfect cup of Coffee!! #Honduras!)
- Examples: Twitter, Foursquare, Gowalla, Yelp, . . .

## Location-based social networks

- LBSNs bridge the gap between the online world and the physical world.
- Two types of user actions:
  - (1) social actions,
  - (2) check-in actions: user links to location.
- Locality of users  
Users tend to visit locations close to their activity space (home, work, . . . ).
- Interests of users  
Users tend to visit locations that match their interests (posts).

## Location-based social networks

- Geographical influence  
Nearby locations have similar check-in probabilities.
- Multinomial distribution does not capture it.
- Use Gaussian distribution.

## Location-based social networks

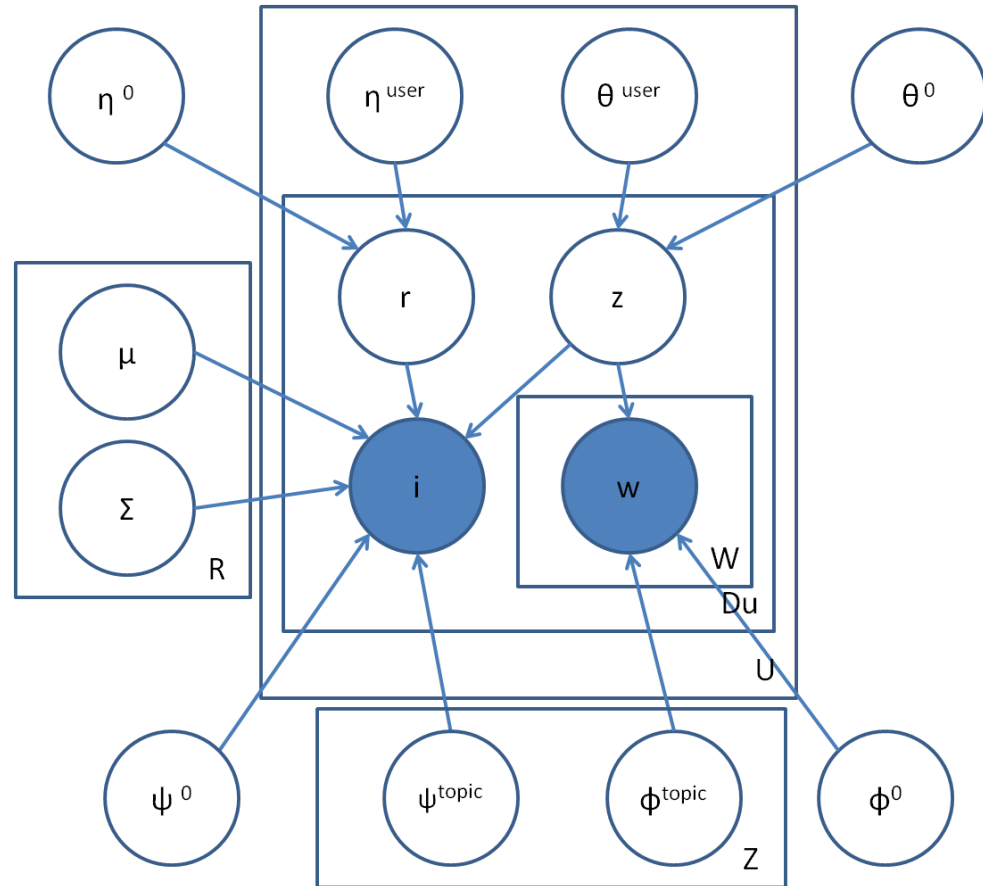
- Text-based location recommendation
  - Given user  $u$  and post (query)  $\{w\}$ .
  - Rank the locations  $i$  w.r.t. the probability  $p_{u,i}$  of  $u$  visiting  $i$ .
- Time-based location recommendation
  - Given user  $u$  and time  $t$ .
  - Rank the locations  $i$  w.r.t. the probability  $p_{u,i}$  of  $u$  visiting  $i$ .

## Location recommendation

- Probabilistic Graphical Model
- Observed variables: locations and words.
- Latent variables:
  - regions with (Gaussian) coordinate distributions,
  - topics with (multinomial) location distributions and word distributions.
- Users associated with region distribution and topic distribution.
- Check-in location depends on
  - region of user,
  - topic (interest) of user.

## Spatial Topic Model

# Spatial Topic Model (ST)



# Spatial Topic Model

To generate a check-in:

- Sample a region
  - User + global region distribution
- Sample a topic
  - User + global topic distribution
- Sample the words
  - Word distribution + global word distribution
- Sample the location
  - Topic's multinomial distribution
  - + region's 2D Gaussian distribution

## Spatial Topic Model

- Sparse coding
- Multiple factors
  - No “switch” variable
  - Model the log-frequency difference from the global distribution
- E.g., for word distributions
  - A global word distribution
  - Topic word distribution (sparse)

## Spatial Topic Model



- Parameter learning
- $P(w, i | \theta)$  hard to be maximized
- Maximize  $P(z, r, w, i | \theta)$
- Monte Carlo EM
  - E step: sample  $z$  and  $r$
  - M step: learn  $\theta$  that maximizes  $P(z, r, w, i | \theta)$
- PSSG (Projected Scaled Sub Gradient)  
[Schmidt et al., AAAI 2007]  
Quasi-Newton with L1 regularization

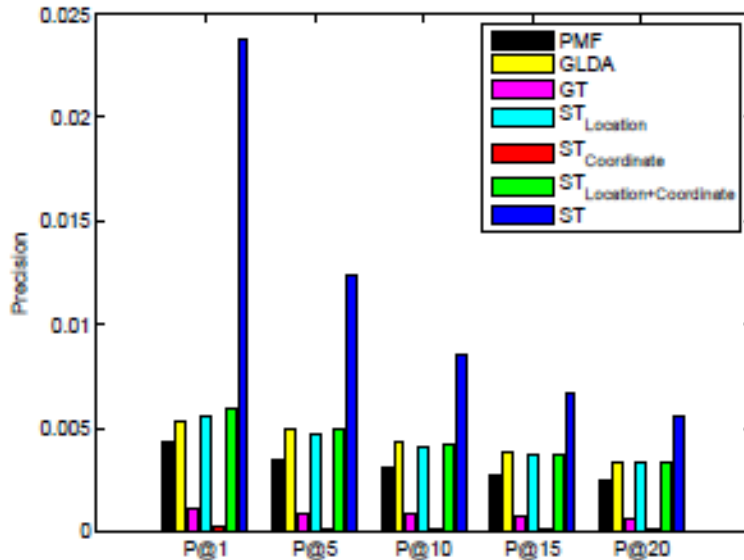
## Spatial Topic Model

## Experimental design

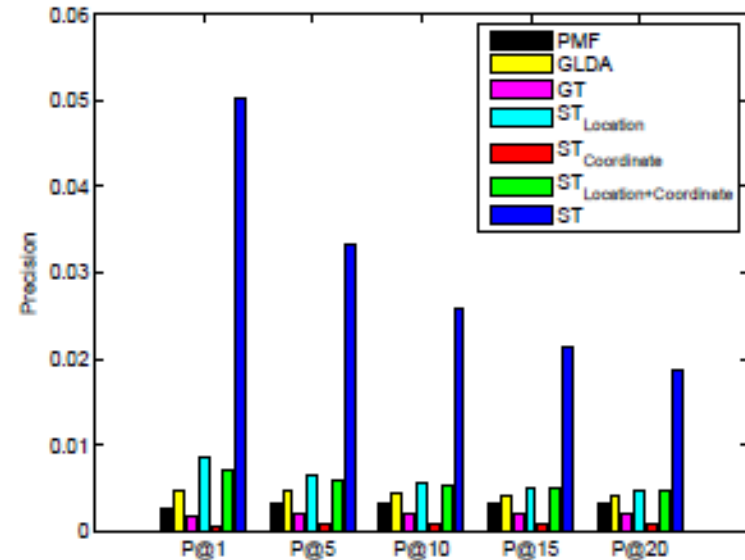
- Data split
  - For each user, 70% check-ins for training, 30% for test
- Recommendation task
  - given user and post
- Evaluation metric: precision@N
  - top N locations are recommended by the model
  - for each test check-in: if the ground truth location is among the recommended N locations:  $1/N$ , otherwise: 0

# Spatial Topic Model

# Experimental results



(a) Twitter data set.



(b) Yelp data set.

## Spatial Topic Model

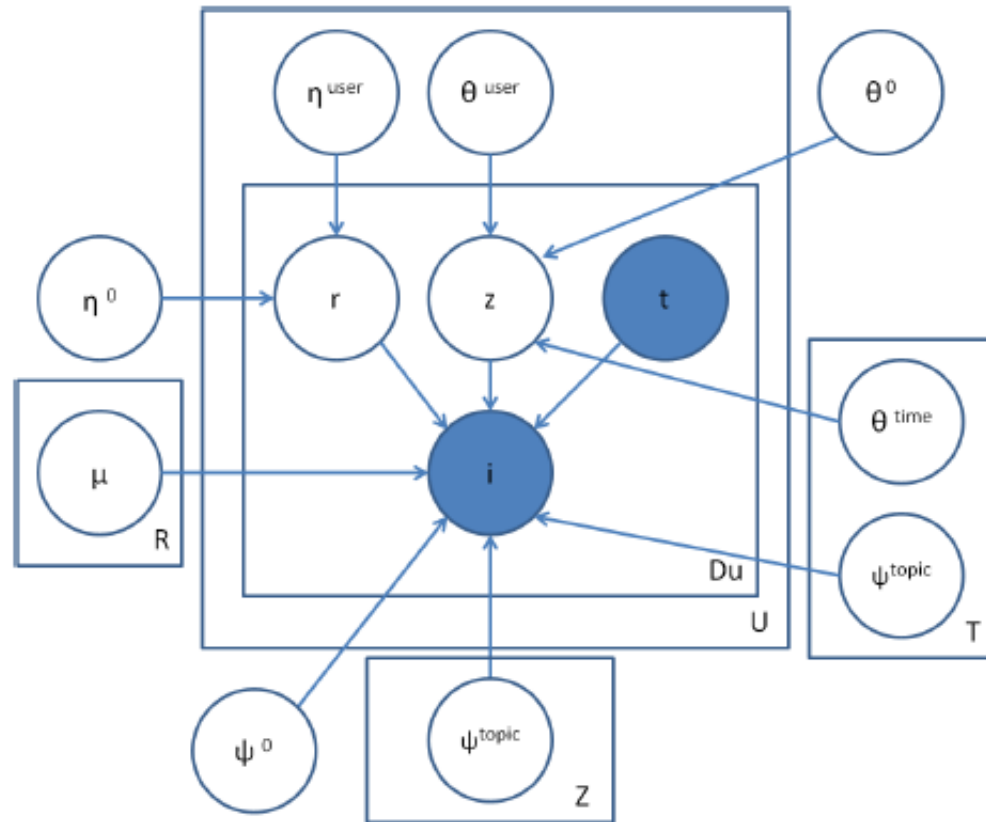
- Why does ST outperform the comparison partners?
- Compared to PMF and GLDA
  - ST also models the text, PMF/GLDA only the location.
    - Use topics to connect users and locations.
- Compared to GT
  - ST models the location (POI), GT only the coordinates.
    - GT only predicts the approximate area, not the exact location.

## Spatial Topic Model

- Check-in location also depends on time, in particular on the relative time, i.e. hour of the day or weekday.
- Discrete time
  - 1-24 (hour)
  - or 1-7 (weekday).
- Check-in location depends on
  - region of user and coordinates of location,
  - topic (interests) of user, and
  - time.

## Spatio-Temporal Topic Model

# Spatio- Temporal Topic Model (STT)



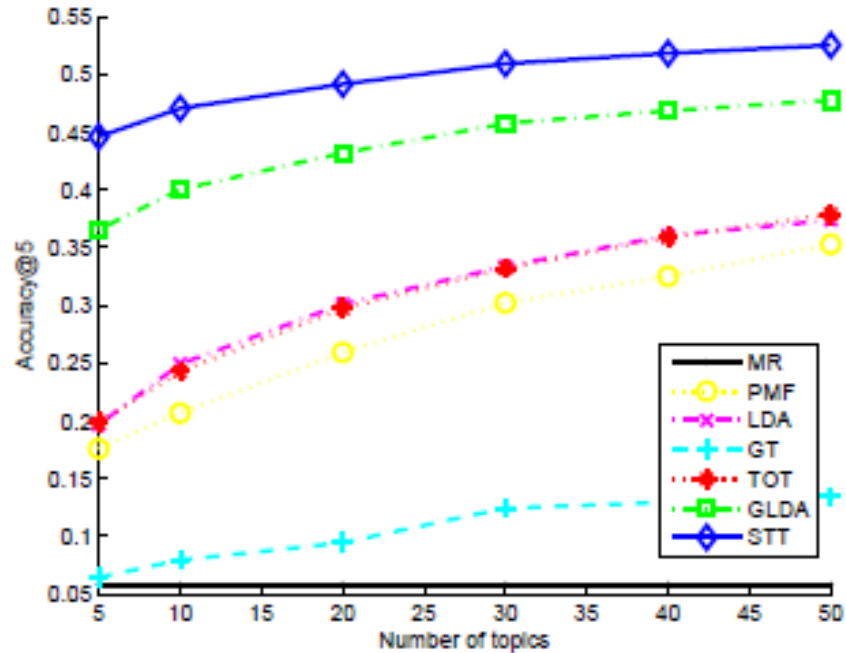
# Spatio-Temporal Topic Model

## Experimental design

- Data split
  - For each user, 70% check-ins for training, 30% for test
- Recommendation task
  - given user and time
- Evaluation metric: accuracy@N
  - top N locations are recommended by the model
  - for each test check-in: if the ground truth location is among the recommended N locations: 1, otherwise: 0

# Spatio-Temporal Topic Model

## Experimental results



# Spatio-Temporal Topic Model



- Why does STT outperform the comparison partners?
- GLDA
  - Does not model the time.
- TOT
  - Does not model the location.
- LDA
  - Does not model the time, does not model geographic distances.
- GT
  - Does not model locations, only coordinates.

## Spatio-Temporal Topic Model

- Inference of latent edge weights  
from observed user interactions
- Recommendation in heterogeneous social networks  
multiple node types
- Explanation of social recommendations  
persuasiveness and informativeness
- Recommendation with trust and distrust information
- Privacy-preserving recommendation in social networks
- Analysis of co-offender networks  
prediction of co-offenders in a crime,  
prediction of crime locations

## Future Work

Martin Ester: Recommendation in Social Networks, Tutorial at RecSys 2013

Mohsen Jamali, Martin Ester: A matrix factorization technique with trust propagation for recommendation in social networks, RecSys 2010.

Mohsen Jamali, Tianle Huang, Martin Ester: A generalized stochastic block model for recommendation in social rating networks, RecSys 2011.

Bo Hu, Martin Ester: Spatial topic modeling in online social media for location recommendation, RecSys 2013

Bo Hu, Mohsen Jamali, Martin Ester: Spatio-Temporal Topic Modeling in Mobile Social Media for Location Recommendation, ICDM 2013

## References